

Homework

- ↳ mailbox #10, 1 PM
- ↳ ground floor of math tower
- ↳ 700 Math tower

1.2.E2: Show if S is a finite semigroup where both cancellation laws hold then S is a group.

goal

- ① Show that $ax=b, ya=b$ are solvable $\forall a, b \in S$.
- ② if the above holds, S is a group.

$$\textcircled{1} \quad \varphi_a : S \rightarrow S \\ x \mapsto ax$$

$$\psi_a : S \rightarrow S \\ y \mapsto ya$$

are injective.
(bc cancellation laws hold)

② Done...

1.3.E4 is $(\mathbb{Q}, +) \cong (\mathbb{Z}, +)$? No.

1.4.E3 - G a gr where $x^2 = e \forall x \in G$, show G is abelian.

$$xy = (xy)^{-1} = y^{-1}x^{-1} = yx$$

- what about $x^3 = e$? No (Heisenberg group).

1.5.E1